



Ohio's Learning Standards
Mathematics
Scope and Sequence
Algebra I

Mathematics Standards Scope and Sequence, Algebra I

Quarter	1		2		3		4	
Unit	1	2	3	4	5	6	7	8
Number and Quantity The Real Number Systems				N.RN.1				
Number and Quantity Quantities	N.Q.1 N.Q.2 N.Q.3				N.Q.1			
Algebra Seeing Structure in Expressions	A.SSE.1 A.SSE.2			A.SSE.2		A.SSE.1	A.SSE.2 A.SSE.3	A.SSE.3
Algebra Arithmetic with Polynomials and Rational Expressions						A.APR.1		
Algebra Creating Equations	A.CED.1 A.CED.4	A.CED.2	A.CED.1 A.CED.2 A.CED.3			A.CED.2	A.CED.1	
Algebra Reasoning with Equations and Inequalities	A.REI.1 A.REI.3	A.REI.10	A.REI.3 A.REI.5 A.REI.6 A.REI.11 A.REI.12			A.REI.4 A.REI.7	A.REI.4	

Mathematics Standards Scope and Sequence, Algebra I

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Functions Building Functions				F.BF.3		F.BF.4		F.BF.1 F.BF.2
Functions Linear, Quadratic, and Exponential Models		F.LE.1 F.LE.2		F.LE.2 F.LE.5				F.LE.1 F.LE.3
Statistics Interpreting Categorical and Quantitative Data		S.ID.7			S.ID.1 S.ID.2 S.ID.3 S.ID.5 S.ID.6 S.ID.8 S.ID.9			
Mathematical Practices	Standards for Mathematical Practices 1-8 should be addressed in every unit throughout the year. Teacher's discretion determines sequence.							
Bold font indicates the first time an assessed standard is introduced in the school year.								

Algebra I – Quarter 1

Unit 1

Number and Quantity – Quantities

N.Q.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays. ★

N.Q.2 Define appropriate quantities for the purpose of descriptive modeling. ★

N.Q.3 Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. ★

Algebra - Seeing Structure in Expressions

A.SSE.1. Interpret expressions that represent a quantity in terms of its context. ★

a. Interpret parts of an expression, such as terms, factors, and coefficients.

b. Interpret complicated expressions by viewing one or more of their parts as a single entity.

A.SSE.2 Use the structure of an expression to identify ways to rewrite it. *For example, to factor $3x(x - 5) + 2(x - 5)$, students should recognize that the " $x - 5$ " is common to both expressions being added, so it simplifies to $(3x + 2)(x - 5)$; or see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$, thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$.*

Algebra I – Quarter 1

Unit 1

Algebra - Creating Equations

A.CED.1 Create equations and inequalities in one variable and use them to solve problems. Include equations and inequalities arising from linear, quadratic, simple rational, and exponential functions. ★

- Focus on applying linear and simple exponential expressions. (A1, M1)
- Focus on applying simple quadratic expressions. (A1, M2)
- Extend to include more complicated function situations with the option to solve with technology. (A2, M3)

A.CED.4 Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. ★

- Focus on formulas in which the variable of interest is linear or square. *For example, rearrange Ohm's law $V = IR$ to highlight resistance R , or rearrange the formula for the area of a circle $A = (\pi)r^2$ to highlight radius r .* (A1)
- Focus on formulas in which the variable of interest is linear. *For example, rearrange Ohm's law $V = IR$ to highlight resistance R .* (M1)
- Focus on formulas in which the variable of interest is linear or square. *For example, rearrange the formula for the area of a circle $A = (\pi)r^2$ to highlight radius r .* (M2)
- While functions will often be linear, exponential, or quadratic, the types of problems should draw from more complicated situations. (A2, M3)

Algebra – Reasoning with Equations and Inequalities

A.REI.1 Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

A.REI.3 Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

Algebra I – Quarter 1

Unit 1

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Algebra I – Quarter 1

Unit 2

Algebra - Creating Equations

A.CED.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. ★

- Focus on applying linear and simple exponential expressions. (A1, M1)
- Focus on applying simple quadratic expressions. (A1, M2)
- Extend to include more complicated function situations with the option to graph with technology. (A2, M3)

Algebra – Reasoning with Equations and Inequalities

A.REI.10 Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line).

Functions - Interpreting Functions

F.IF.1 Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then $f(x)$ denotes the output of f corresponding to the input x . The graph of f is the graph of the equation $y = f(x)$.

F.IF.2 Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

F.IF.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. *Key features include the following: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* ★ (A2, M3)

- Focus on linear and exponential functions. (M1)
- Focus on linear, quadratic, and exponential functions. (A1, M2)

Unit 2

Functions - Interpreting Functions

F.IF.5 Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. *For example, if the function $h(n)$ gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.* ★

- Focus on linear and exponential functions. (M1)
- Focus on linear, quadratic, and exponential functions. (A1, M2)
- Emphasize the selection of a type of function for a model based on behavior of data and context. (A2, M3)

F.IF.6 Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. ★ (A2, M3)

F.IF.7 Graph functions expressed symbolically and indicate key features of the graph, by hand in simple cases and using technology for more complicated cases. Include applications and how key features relate to characteristics of a situation, making selection of a particular type of function model appropriate. ★

- Graph linear functions and indicate intercepts. (A1, M1)
- Graph quadratic functions and indicate intercepts, maxima, and minima. (A1, M2)
- Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions. (A2, M3)
- Graph polynomial functions, identifying zeros, when factoring is reasonable, and indicating end behavior. (A2, M3)
- Graph simple exponential functions, indicating intercepts and end behavior. (A1, M1)
- f. (+)** Graph exponential functions, indicating intercepts and end behavior, and trigonometric functions, showing period, midline^G, and amplitude. (A2, M3)
- Graph rational functions, identifying zeros and asymptotes when factoring is reasonable, and indicating end behavior. (A2, M3)
- h. (+)** Graph logarithmic functions, indicating intercepts and end behavior.

F.IF.9 Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). *For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.* (A2, M3)

- Focus on linear and exponential functions. (M1)
- Focus on linear, quadratic, and exponential functions. (A1, M2)

Algebra I – Quarter 1

Unit 2

Functions - Linear, Quadratic, and Exponential Models

F.LE.1 Distinguish between situations that can be modeled with linear functions and with exponential functions.★

- a. Show that linear functions grow by equal differences over equal intervals and that exponential functions grow by equal factors over equal intervals.
- b. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.
- c. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.

F.LE.2 Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).★

Statistics - Interpreting Categorical and Quantitative Data

S.ID.7 Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.★

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Algebra I – Quarter 2

Unit 3

Algebra - Creating Equations

A.CED.1 Create equations and inequalities in one variable and use them to solve problems. Include equations and inequalities arising from linear, quadratic, simple rational, and exponential functions. ★

- a. Focus on applying linear and simple exponential expressions. (A1, M1)
- b. Focus on applying simple quadratic expressions. (A1, M2)
- c. Extend to include more complicated function situations with the option to solve with technology. (A2, M3)

A.CED.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. ★

- a. Focus on applying linear and simple exponential expressions. (A1, M1)
- b. Focus on applying simple quadratic expressions. (A1, M2)
- c. Extend to include more complicated function situations with the option to graph with technology. (A2, M3)

A.CED.3 Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context. *For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.* ★ (A1, M1)

- a. While functions will often be linear, exponential, or quadratic, the types of problems should draw from more complicated situations. (A2, M3)

Algebra I – Quarter 2

Unit 3

Algebra – Reasoning with Equations and Inequalities

A.REI.3 Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

A.REI.5 Verify that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.

A.REI.6 Solve systems of linear equations algebraically and graphically.

a. Limit to pairs of linear equations in two variables. (A1, M1)

b. Extend to include solving systems of linear equations in three variables, but only algebraically. (A2, M3)

A.REI.11 Explain why the x-coordinates of the points where the graphs of the equation $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$; find the solutions approximately, e.g., using technology to graph the functions, making tables of values, or finding successive approximations.

A.REI.12 Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Algebra I – Quarter 2

Unit 4

Number and Quantity - The Real Number Systems

N.Q.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays. ★

Algebra - Seeing Structure in Expressions

A.SSE.2 Use the structure of an expression to identify ways to rewrite it. *For example, to factor $3x(x - 5) + 2(x - 5)$, students should recognize that the " $x - 5$ " is common to both expressions being added, so it simplifies to $(3x + 2)(x - 5)$; or see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$, thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$.*

Functions - Interpreting Functions

F.IF.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. *Key features include the following: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* ★ (A2, M3)

- a. Focus on linear and exponential functions. (M1)
- b. Focus on linear, quadratic, and exponential functions. (A1, M2)

Unit 4

Functions - Interpreting Functions

F.IF.7 Graph functions expressed symbolically and indicate key features of the graph, by hand in simple cases and using technology for more complicated cases. Include applications and how key features relate to characteristics of a situation, making selection of a particular type of function model appropriate. ★

- a. Graph linear functions and indicate intercepts. (A1, M1)
- b. Graph quadratic functions and indicate intercepts, maxima, and minima. (A1, M2)
- c. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions. (A2, M3)
- d. Graph polynomial functions, identifying zeros, when factoring is reasonable, and indicating end behavior. (A2, M3)
- e. Graph simple exponential functions, indicating intercepts and end behavior. (A1, M1)
- f. (+)** Graph exponential functions, indicating intercepts and end behavior, and trigonometric functions, showing period, midline^G, and amplitude. (A2, M3)
- g. Graph rational functions, identifying zeros and asymptotes when factoring is reasonable, and indicating end behavior. (A2, M3)

F.IF.8 Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.

- a. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. (A2, M3)
 - i. Focus on completing the square to quadratic functions with the leading coefficient of 1. (A1, M2)
- b. Use the properties of exponents to interpret expressions for exponential functions. *For example, identify percent rate of change^G in functions such as $y = (1.02)^t$, and $y = (0.97)^t$ and classify them as representing exponential growth or decay.* (A2, M3)
 - i. Focus on exponential functions evaluated at integer inputs. (A1, M2)

Algebra I – Quarter 2

Unit 4

Functions - Building Functions

F.BF.3 Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $kf(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them. (A2, M3)

a. Focus on transformations of graphs of quadratic functions, except for $f(kx)$; (A1, M2)

Functions - Linear, Quadratic, and Exponential Models

F.LE.2 Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table). ★

F.LE.5 Interpret the parameters in a linear or exponential function in terms of a context. ★

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Algebra I – Quarter 3

Unit 5

Number and Quantity – Quantities

N.Q.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays. ★

Statistics - Interpreting Categorical and Quantitative Data

S.ID.1 Represent data with plots on the real number line (dot plots^G, histograms, and box plots) in the context of real-world applications using the GAISE model. ★

S.ID.2 In the context of real-world applications by using the GAISE model, use statistics appropriate to the shape of the data distribution to compare center (median and mean) and spread (mean absolute deviation^G, interquartile range^G, and standard deviation) of two or more different data sets. ★

S.ID.3 In the context of real-world applications by using the GAISE model, interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers). ★

S.ID.5 Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data. ★

S.ID.6 Represent data on two quantitative variables on a scatter plot, and describe how the variables are related. ★

a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. *Use given functions, or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.* (A2, M3)

b. Informally assess the fit of a function by discussing residuals. (A2, M3)

c. Fit a linear function for a scatterplot that suggests a linear association. (A1, M1)

S.ID.8 Compute (using technology) and interpret the correlation coefficient of a linear fit. ★

S.ID.9 Distinguish between correlation and causation. ★

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Algebra I – Quarter 3

Unit 6

Algebra - Seeing Structure in Expressions

A.SSE.1 Interpret expressions that represent a quantity in terms of its context. ★

- Interpret parts of an expression, such as terms, factors, and coefficients.
- Interpret complicated expressions by viewing one or more of their parts as a single entity.

Algebra - Arithmetic with Polynomials and Rational Expressions

A.APR.1 Understand that polynomials form a system analogous to the integers, namely, that they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.

- Focus on polynomial expressions that simplify to forms that are linear or quadratic. (A1, M2)
- Extend to polynomial expressions beyond those expressions that simplify to forms that are linear or quadratic. (A2, M3)

Algebra - Creating Equations

A.CED.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. ★

- Focus on applying linear and simple exponential expressions. (A1, M1)
- Focus on applying simple quadratic expressions. (A1, M2)
- Extend to include more complicated function situations with the option to graph with technology. (A2, M3)

Algebra I – Quarter 3

Unit 6

Algebra – Reasoning with Equations and Inequalities

A.REI.4 Solve quadratic equations in one variable.

- Use the method of completing the square to transform any quadratic equation in x into an equation of the form $(x - p)^2 = q$ that has the same solutions.
- Solve quadratic equations as appropriate to the initial form of the equation by inspection, e.g., for $x^2 = 49$; taking square roots; completing the square; applying the quadratic formula; or utilizing the Zero-Product Property after factoring
- (+) Derive the quadratic formula using the method of completing the square.

A.REI.7 Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. *For example, find the points of intersection between the line $y = -3x$ and the circle $x^2 + y^2 = 3$.*

Functions - Interpreting Functions

F.IF.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. *Key features include the following: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.* ★ (A2, M3)

- Focus on linear and exponential functions. (M1)
- Focus on linear, quadratic, and exponential functions. (A1, M2)

Algebra I – Quarter 3

Unit 6

Functions - Interpreting Functions

F.IF.7 Graph functions expressed symbolically and indicate key features of the graph, by hand in simple cases and using technology for more complicated cases. Include applications and how key features relate to characteristics of a situation, making selection of a particular type of function model appropriate. ★

- a. Graph linear functions and indicate intercepts. (A1, M1)
- b. Graph quadratic functions and indicate intercepts, maxima, and minima. (A1, M2)
- c. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions. (A2, M3)
- d. Graph polynomial functions, identifying zeros, when factoring is reasonable, and indicating end behavior. (A2, M3)
- e. Graph simple exponential functions, indicating intercepts and end behavior. (A1, M1)
- f. (+) Graph exponential functions, indicating intercepts and end behavior, and trigonometric functions, showing period, midline^G, and amplitude. (A2, M3)
- g. Graph rational functions, identifying zeros and asymptotes when factoring is reasonable, and indicating end behavior. (A2, M3)

Functions - Building Functions

F.BF.4 Find inverse functions.

- a. (+) Informally determine the input of a function when the output is known. (A1, M1)
- b. (+) Read values of an inverse function from a graph or a table, given that the function has an inverse. (A2, M3)
- c. (+) Verify by composition that one function is the inverse of another. (A2, M3)
- d. (+) Find the inverse of a function algebraically, given that the function has an inverse. (A2, M3)
- e. (+) Produce an invertible function from a non-invertible function by restricting the domain.

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Algebra I – Quarter 4

Unit 7

Algebra - Seeing Structure in Expressions

A.SSE.2 Use the structure of an expression to identify ways to rewrite it. *For example, to factor $3x(x - 5) + 2(x - 5)$, students should recognize that the " $x - 5$ " is common to both expressions being added, so it simplifies to $(3x + 2)(x - 5)$; or see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$, thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$.*

A.SSE.3 Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. ★

- Factor a quadratic expression to reveal the zeros of the function it defines. (A1, M2)
- Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines. (A1, M2)
- Use the properties of exponents to transform expressions for exponential functions. For example, 8^t can be written as 2^{3t} .

Algebra - Creating Equations

A.CED.1 Create equations and inequalities in one variable and use them to solve problems. Include equations and inequalities arising from linear, quadratic, simple rational, and exponential functions. ★

- Focus on applying linear and simple exponential expressions. (A1, M1)
- Focus on applying simple quadratic expressions. (A1, M2)
- Extend to include more complicated function situations with the option to solve with technology. (A2, M3)

Algebra I – Quarter 4

Unit 7

Algebra – Reasoning with Equations and Inequalities

A.REI.4 Solve quadratic equations in one variable.

- a. Use the method of completing the square to transform any quadratic equation in x into an equation of the form $(x - p)^2 = q$ that has the same solutions.
- b. Solve quadratic equations as appropriate to the initial form of the equation by inspection, e.g., for $x^2 = 49$; taking square roots; completing the square; applying the quadratic formula; or utilizing the Zero-Product Property after factoring
- c. (+) Derive the quadratic formula using the method of completing the square.

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Unit 8

Algebra - Seeing Structure in Expressions

A.SSE.3 Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. ★

- a. Factor a quadratic expression to reveal the zeros of the function it defines. (A1, M2)
- b. Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines. (A1, M2)
- c. Use the properties of exponents to transform expressions for exponential functions. For example, 8^t can be written as 2^{3t} .

Functions - Interpreting Functions

F.IF.3 Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. *For example, the Fibonacci sequence is defined recursively by $f(0) = f(1) = 1$, $f(n + 1) = f(n) + f(n - 1)$ for $n \geq 1$.*

F.IF.8 Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.

- a. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. (A2, M3)
 - i. Focus on completing the square to quadratic functions with the leading coefficient of 1. (A1, M2)
- b. Use the properties of exponents to interpret expressions for exponential functions. *For example, identify percent rate of change^G in functions such as $y = (1.02)^t$, and $y = (0.97)^t$ and classify them as representing exponential growth or decay.* (A2, M3)
 - i. Focus on exponential functions evaluated at integer inputs. (A1, M2)

Algebra I – Quarter 4

Unit 8

Functions - Building Functions

F.BF.1 Write a function that describes a relationship between two quantities.★

- a. Determine an explicit expression, a recursive process, or steps for calculation from context.
 - i. Focus on linear and exponential functions. (A1, M1)
 - ii. Focus on situations that exhibit quadratic or exponential relationships. (A1, M2)
- b. Combine standard function types using arithmetic operations. *For example, build a function that models the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these functions to the model.* (A2, M3)
- c. (+) Compose functions. *For example, if $T(y)$ is the temperature in the atmosphere as a function of height, and $h(t)$ is the height of a weather balloon as a function of time, then $T(h(t))$ is the temperature at the location of the weather balloon as a function of time.*

F.BF.2 Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.★

Functions - Linear, Quadratic, and Exponential Models

F.LE.1 Distinguish between situations that can be modeled with linear functions and with exponential functions.★

- a. Show that linear functions grow by equal differences over equal intervals and that exponential functions grow by equal factors over equal intervals.
- b. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.
- c. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.

F.LE.3 Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly or quadratically. ★ (A1, M2)

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.